MONTE CARLO SIMULATION-BASED DOSIMETRIC EVALUATION OF A NOVEL ¹²⁵I BRACHYTHERAPY SOURCE Comparative Assessment of Dosimetry Parameters and Shadowing Effects

by

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This study investigates a novel ¹²⁵I radiotherapy source. It evaluates its dosimetric parameters using Monte Carlo simulation around the source, following the updated American Association of Physicists in Medicine Task Group recommendations. For this new source configuration, the dose rate constant Λ , geometry function $G(r, \theta)$, radial dose function $g_L(r)$, and anisotropy function $F(r, \theta)$, were determined using Geant4 Monte Carlo simulations. Additionally, a comparison of the obtained dosimetric parameters with those of an earlier ¹²⁵I source model was conducted to analyze the shadowing effect between the two designs during multi-source brachytherapy implants.

Key words: brachytherapy, Geant4, Monte Carlo simulation, capsule structure

INTRODUCTION

Nowadays, brachytherapy is widely used to treat various types of cancers, including oral, prostate, cervix, breast, skin, neck, and other cancers. Brachytherapy sources are primarily classified into two categories: high-dose-rate (HDR) and low-dose-rate (LDR) sources. Radioactive isotopes such as ¹²⁵I, ¹⁰³Pd, and ¹³¹Cs are commonly preferred for LDR brachytherapy due to their low energy levels, short half-lives, and material versatil-ity [1-4].

Before starting radiotherapy treatment, it is essential to enhance and validate dosimetric parameters such as the dose rate constant, geometry function, radial dose function, and anisotropy function around the brachytherapy seed. This can be achieved experimentally or through simulation [5, 6]. Monte Carlo (MC) simulation codes are especially valuable for modeling brachytherapy sources. They effectively simulate the geometry of these sources, the physics of radiation interacting with matter, and the process of dose absorption. A significant advantage of these simulations is their ability to provide dose data at locations where experimental measurements are difficult or impractical to obtain [7, 8]. There are many MC simulation codes capable of modeling source geometry, radiation interaction, and dose absorption in cells [9-11]. Among these, Geant4 stands out due to its exceptional capability in constructing and handling various designs of radioactive sources. Geant4, developed by CERN (the European Organization for Nuclear Research), is one of the most powerful simulation codes available. It provides a comprehensive description of experiments and supports the extraction of data necessary for simulations [12, 13].

This study aims to characterize the dosimetric parameters of a novel ¹²⁵I brachytherapy source using Geant4 MC simulations, adhering to the updated American Association of Physicists (AAPM) Task Group recommendations. The specific objectives are to determine the dose rate constant, geometry function, radial dose function, and anisotropy function, and to compare these parameters with a previous ¹²⁵I source model to evaluate the shadowing effect in multi-source brachytherapy implants.

MATERIAL AND METHODS

Geant4 MC simulations

Geant4 is a simulation toolkit built on C++ class libraries, widely used in high-energy physics, space radiation modeling, and medical physics. Developed

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in 1998 by CERN, it employs object-oriented programming and MC methods to simulate particle interactions with matter. The toolkit enables users to define complex geometries and materials, track particles using robust physical models, visualize interactions, and generate simulated data. By integrating experimental and theoretical models, Geant4 provides a comprehensive understanding of particle-material interactions across a wide energy range, making it a preferred choice for complex simulations over traditional MC codes [12, 13].

The geometry and source arrangements are coded in the mandatory Geant4 class DetectorConstruction.cc. Physics processes are defined in PhysListEmLowEnergy.cc, where the following interactions are implemented: For gamma rays: Compton scattering, photoelectric absorption, pair production, and Rayleigh (coherent) scattering. For electrons and positrons: multiple scattering, ionization, and bremsstrahlung. All classes are designed with object-oriented programming principles in C++ and include comprehensive routines for handling complex tasks. The G4RunManager class acts as the maestro, controlling all actions and initializing the simulation setup by coordinating the execution of all arrangements.

Source description

The specifications of the currently investigated ¹²⁵I seed are shown in fig. 1. The ¹²⁵I source features rounded ends. The seed encapsulation has a total length of 4.8 mm (0.3 mm longer than the previous design) and is constructed from titanium with a 0.05 mm wall thickness (0.05 mm thinner). The total length of seed encapsulation is equal to 4.6 mm and is made of titanium ($\rho = 4.54$ gcm⁻³) with 0.05 mm thickness that contains a palladium core having a 3.5 mm active length, with 0.6 mm thick end. In contrast, our previous brachytherapy source design contained four polystyrene ion-exchange resin beads and two centrally positioned radiographic markers composed of an 80% gold and 20% copper alloy.

Simulations assumed 40 % relative humidity and an air density of 0.00120 gcm⁻³. The dry air composition (by mass percentage) was defined as H: 0.0732 %, C: 0.0123 %, N: 75.0325 %, O: 23.6077 %, and Ar: 1.2743 %. The atomic number and density of elements used in the¹²⁵I brachytherapy sources are provided in tab. 1.



Figure 1. Simulated model of ¹²⁵I brachytherapy source

 Table 1. Atomic number and density of elements used in the ¹²⁵I seeds

Element	Proton number (Z)	Density [gcm ⁻¹]	
Iodine (I)	53	4.93	
Titanium (Ti)	22	4.51	
Palladium (Pd)	46	12.02	
Copper (Cu)	29	8.92	
Gold (Au)	79	19.32	

Dose rate constant Λ

Dose rate constant Λ is the ratio of dose rate $\dot{D}(r_0, \theta_0)$ [cGyh¹] in water at $r_0 = 1$ cm, from the source center on the transverse plane and $\theta_0 = 90^\circ$ to the air kerma strength S_K

$$\Lambda = \frac{D(r_0, \theta_0)}{S_K} \tag{1}$$

The air-kerma strength S_K is the product of the air kerma rate K_d [µGyh⁻¹] and the square of the distance d to the point of specification

$$S_K = K_d d^2 \tag{2}$$

It is expressed in Gys⁻¹ but in a more convenient way especially for low-dose rate brachytherapy, in μ Gyh⁻¹, at 1 m. For convenience, μ Gym²h⁻¹ is denoted by the symbol U where 1U = cGycm²h⁻¹ = μ Gym²h⁻¹. So, the dose rate constant Λ has the unit of cGyh¹U⁻¹. To calculate the air kerma strength of the ¹²⁵ I capsule, an air sphere ring with a thickness 0.01 cm was used to detect the absorbed dose as shown in fig. 2.

Radial dose function calculation

Radial dose function considers dose reduction due to photon attenuation and scattering in the medium. According to AAPM [14], the radial dose function g(r) is defined as

$$g_L(r) = \frac{\dot{D}(r,\theta_0) G_L(r_0,\theta_0)}{\dot{D}(r_0,\theta_0) G_L(r,\theta_0)}$$
(3)



Figure 2. Dose rate calculation geometry at 1 cm from the source's center



Figure 3. Co-ordinate system used for brachytherapy dosimetry calculations

where *L* represents the length of the active source, θ is the polar angle as shown in fig. 3. The $\dot{D}(r_0, \theta_0)$ and $\dot{D}(r, \theta_0)$ are dose rates measured away from the source center; the $G_L(r_0, \theta_0)$ and $G_L(r, \theta_0)$ are the geometry functions on the transverse plane at 1 cm and *r* in cm, respectively.

Geometry function

The geometry function $G(r, \theta)$ [cm⁻²] is calculated by the following formulas

$$G(r,\theta) = \begin{pmatrix} \frac{\theta_2 - \theta_1}{Lr\sin(\theta)}, & \text{if } \theta \neq 0\\ \left(r^2 - \frac{L^2}{4}\right)^{-1}, & \text{if } \theta \neq 0 \end{pmatrix}$$
$$\beta = \theta_2 - \theta_1 = \left(\frac{r\sin(\theta)}{r\cos(\theta) - \frac{1}{2}L}\right) - \tan^{-1} \left(\frac{r\sin(\theta)}{r\cos(\theta) + \frac{1}{2}L}\right)$$
(4)

Anisotropy function

According to the AAPM [14], the anisotropy function describes the anisotropy of dose distribution around the seed. It is defined as the angular dependence of photon scattering and attenuation in encapsulating layers and media

$$F(r,\theta) = \frac{D(r,\theta)G_L(r_0,\theta_0)}{\dot{D}(r_0,\theta_0)G_L(r,\theta)}$$
(5)

Absorbed dose

The general, 2-D equation of the absorbed dose $D(r, \theta)$ at a point from a brachytherapy source is [14]

$$D(r,\theta) = S_k A G(r,\theta) F(r,\theta) t$$
(6)

where r – the distance from the center of the active source to the point of interest, θ – the polar angle specifying the point of interest, relative to the source longitudinal axis, and t – the time of exposure. In multi-source brachytherapy implant



Figure 4. Simple method for calculating ISE for current and earlier ¹²⁵I brachytherapy sources

scenarios, the intensity of photons emitted from each seed into the treatment volume may be reduced due to the shadowing effect from neighboring seeds. This inter-seed effect (ISE), dimensionless quantity, between brachytherapy sources can be quantified using the following equation [14]

$$ISE = \frac{D_{12}}{D_1 + D_2}$$
(7)

where D_{12} is the absorbed dose at a given point inside the dosimetry medium caused by the two seeds implants, D_1 and D_2 – the absorbed dose at the same point due to the separate presence of source 1 and source 2. The geometrical arrangement for ISE evaluation is shown in fig. 4.

RESULTS AND DISCUSSION

In this study, the dosimetric properties of the ¹²⁵I brachytherapy source were analyzed using Geant4based MC simulations. The simulation results were compared with previously published data from our earlier paper [9] and other studies, including the ¹²⁵I-6711 [15], ¹²⁵I-BT [16], ¹²⁵I-IRA [17], and ¹²⁵I-MED3631A/M [18] sources. In this experiment, a dose-rate constant of (0.925 ± 0.019) cGyh⁻¹U⁻¹ was calculated for the encapsulated source design using MC simulations. When compared to published data for other commercial ¹²⁵I brachytherapy sources tab. 2, the results demonstrate minimal discrepancies between the values obtained in this study and established reference data.

Table 2. Comparison of dose rate constant $\Lambda,$ with other $^{125}\!I$ seeds

Source (¹²⁵ I seeds)	Dose-rate constant [cGyh ⁻¹ U ⁻¹]		
¹²⁵ I-MED3631A/M [18].	1.067		
125I-6711 [15]	0.942 ± 1.76		
¹²⁵ I-BT [16]	0.928 ±0.01		
¹²⁵ I-IRA [17]	1.068		
Our previous paper [9]	0.925 ±0.019		
Current work			

	$g_{\rm L}(r)$					
Distance r [cm]	¹²⁵ I-MED3631A/M [18]	¹²⁵ I-6711 [15]	¹²⁵ I-BT [16]	¹²⁵ I-IRA[17]	Previous paper [9]	Current work
	MCNP	MCNP	MCNP	MCNP	Geant4	Geant4
0.25	0.992	_	_	1.102	1.007	0.998
0.30	1.002	-	_	_	1.005	1.004
0.35	1.008	-	—	_	1.010	1.007
0.40	1.012	-	_	_	1.018	1.016
0.50	1.015	1.07	1.074	1.075	1.017	1.015
0.60	1.016	-	_	_	1.021	1.018
0.75	1.014	1.025	1.025	1.042	1.019	1.016
1.00	1.000	1.000	1.000	1.000	1.013	1.013
1.25	0.977	-	_	_	1.002	0.973
1.50	0.948	0.908	0.914	0.914	0.968	0.943
1.75	0.917	-	_	_	0.936	0.917
2.00	0.883	0.814	0.822	0.819	0.84	0.883
2.50	0.810	-	_	_	0.768	0.814
3.00	0.733	0.633	0.645	0.643	0.697	0.735
4.00	0.590	0.482	0.496	0.492	0.565	0.594
5.00	0.466	0.361	0.379	0.37	0.432	0.436
7.00	0.277	0.199	0.212	0.205	0.256	0.267
10.00	0.121	-	-	_	0.112	0.115

Table 3. Comparison of radial dose function, with other ¹²⁵I seeds

The radial dose function, $g_L(r)$, was calculated over a distance range of 0.25 cm to 10 cm from the source center using the Geant4 MC toolkit. The results showed a notably strong agreement with published data for other commercial ¹²⁵I brachytherapy sources, tab. 3. Additionally, the simulated radial dose function, g(r), for the ¹²⁵I source was compared to both prior ¹²⁵I seed designs and our earlier work, as illustrated in fig. 4.

As shown in fig. 5, the radial dose function values of the model closely match those of the reference data in the regions 0 < r < 1 cm and 6 < r < 10.0 cm. Nevertheless, moderate deviations are observed within the intermediate range (1 < r < 6 cm). Compared to published data for commercial ¹²⁵I seeds, the differences between the model's results and the reference data are negligible, indicating good agreement across most radial distances.

Anisotropy functions were calculated at radial distances ranging from 0.25 cm to 10 cm and at angles



Figure 5. Simulation of radial dose function compared to other studies

spanning 0° to 180° around the source. The resulting anisotropy function values are summarized in tab. 4, and their graphical representation for the ¹²⁵I source is provided in fig. 6. Smooth variations in anisotropy function values were observed across all evaluated angles around the brachytherapy source.

Finally, we evaluated ISE of the current ¹²⁵I brachytherapy source and our previous source at distances from 1 cm to 7 cm, in increments of 0.5 cm. As illustrated in fig. 7, ISE values at distances greater than 3.5 cm converge, resulting in a flattened trend of ISE variations at far distances from the multi-seed implant. This phenomenon likely arises from the increased contribution of scattered radiation to the absorbed dose at larger distances, which counterbalances attenuation effects. The interplay between scattering and attenuation ultimately leads to the observed plateau in ISE trends at far distances.

CONCLUSION

In this study, the updated ¹²⁵I brachytherapy source was validated using a Geant4 MC simulation code. The source geometry was modeled, and key AAPM-recommended dosimetric parameters-including the dose rate constant, geometry function, radial dose function, and anisotropy function-were calculated for the source. These results were compared with data from our earlier design and published values for commercial ¹²⁵I sources. The computed parameters were within clinically acceptable tolerances, confirming that the updated source provides a dosimetric distribution that meets clinical standards. Additionally, the ISE between the current and earlier source designs was evaluated to quantify the shadowing effect in

	Simulated $F(r, \theta)$						
Polar angle (θ°)	<i>r</i> [cm]						
	0.25	0.50	1.00	2.00	5.00	10.00	
0°	0.813	0.625	0.624	0.650	0.699	0.689	
10°	0.833	0.780	0.761	0.790	0.744	0.756	
20°	0.863	0.866	0.789	0.799	0.823	0.843	
30°	0.888	0.846	0.886	0.851	0.886	0.881	
40°	0.886	0.891	0.922	0.907	0.918	0.933	
50°	0.943	0.931	0.915	0.914	0.942	0.941	
60°	0.961	0.950	0.970	0.973	0.978	0.988	
70°	1.001	0.985	0.955	0.957	0.957	0.953	
80°	1.010	0.980	1.008	0.998	1.001	0.999	
90°	1.000	1.000	1.000	1.000	1.000	1.000	
100°	1.007	0.990	0.991	1.000	1.004	0.978	
110°	0.979	0.967	0.967	0.978	0.987	0.989	
120°	0.956	0.933	0.945	0.967	0.956	0.977	
130°	0.931	0.901	0.926	0.967	0.966	0.933	
140°	0.888	0.895	0.889	0.904	0.901	0.883	
150°	0.840	0.801	0.810	0.833	0.852	0.861	
160°	0.733	0.691	0.701	0.712	0.767	0.789	
170°	0.715	0.620	0.676	0.666	0.701	0.723	
180°	0.644	0.623	0.677	0.667	0.700	0.715	

Table 4. Simulation for anisotropy function of the designed ¹²⁵I source from 0° to 180°



Figure 6. Geant 4 MC simulations for $F(r, \theta)$

multi-source implant configurations. The ISE values converge at distances beyond 3.5 cm, resulting in a flattened dose trend at larger radial distances. This behavior is attributed to the interplay between scattered radiation (which increases with distance) and attenuation effects, ultimately stabilizing dose variations in multi-source implants.

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Figure 7. The values of inter-seed effect at different distances from the current ¹²⁵I brachytherapy source and our previous source

AUTHORS' CONTRIBUTIONS

W. Duo: building simulation configuration, writing the original manuscript, and project administration. W. Shuahua: literature review, running simulations, data analysis, correcting manuscript, and project administration. O. M. Mostafa: literature review, conducting simulations, and data analysis. M. E. Medhat: proposing the research idea and developing the theoretical framework.

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ДОЗИМЕТРИЈСКА ПРОЦЕНА НОВОГ ¹²⁵І БРАХИТЕРАПИЈСКОГ ИЗВОРА ЗАСНОВАНА НА МОНТЕ КАРЛО СИМУЛАЦИЈИ Компаративна процена дозиметријских параметара и ефеката заклањања

Користећи Монте Карло симулацију око извора и пратећи ажуриране препоруке радне групе Америчког удружења физичара у медицини, истраживан је нови извор за радиотерапију¹²⁵I. За ову нову конфигурацију извора, константа брзине дозе Λ , геометријска функција $G(r, \theta)$, функција радијалне дозе $g_L(r)$ и функција анизотропије $F(r, \theta)$, одређене су коришћењем Geant4 Монте Карло симулације. Поред тога, спроведено је поређење добијених дозиметријских параметара са онима из ранијег модела извора¹²⁵I, да би се анализирао ефекат заклањања између два дизајна током имплантата брахитерапије са више извора.

Кључне речи: брахишераџија, Geant4 Монше Карло симулација, кайсуларна сшрукшура